

# Florida Department of Transport APT and Instrumentation Workshop



Granular base/subbase layers:  
Combining laboratory and HVS data

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# Structure of presentation

- Background and general comments
- Modeling the behaviour of granular pavement layers
  - Non-linear resilient modulus
  - Shear strength
  - Plastic deformation
- A comparison between laboratory and HVS permanent deformation models



# **Background and general comments**

Granular base/subbase layers:  
Combining laboratory and HVS data

# Why permanent deformation of unbound material?

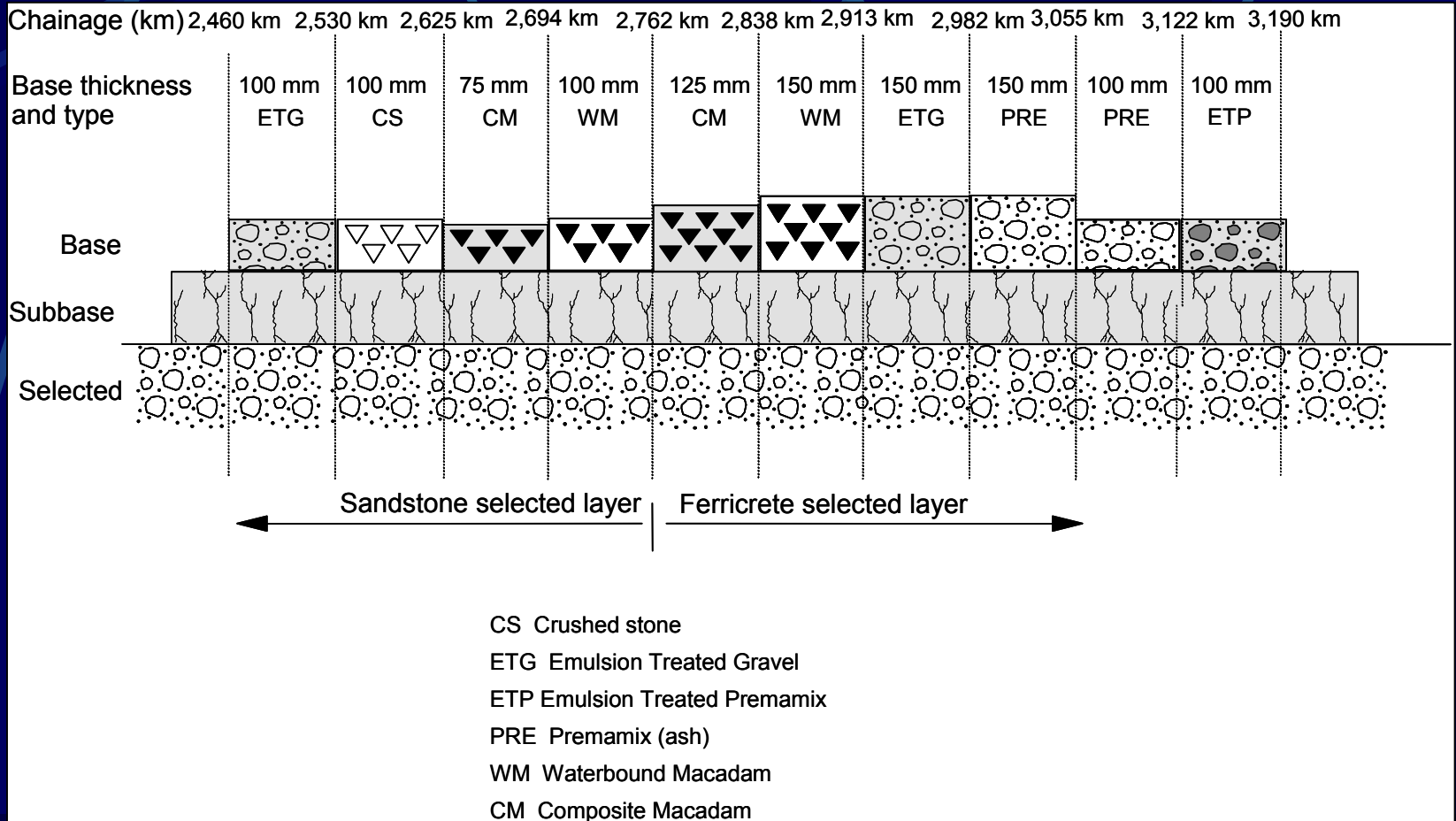
- Thin (25 – 50 mm) AC on unbound base layers
- 40 – 60 % of rut from permanent deformation of unbound base layers
- All pavement materials and layers deform permanently under repeated loading

# Background

- Labour-intensive road construction to create employment
  - “Unconventional” material
- Process applied to
  - Waterbound macadam
  - Clinker ash waste product
  - Natural gravel
  - Crushed stone



# Layout of experimental sections



**ROAD D2388 EXPERIMENTAL SECTIONS**



# **Resilient response**

Granular base/subbase layers:  
Combining laboratory and HVS data

# Non-linear resilient modulus models

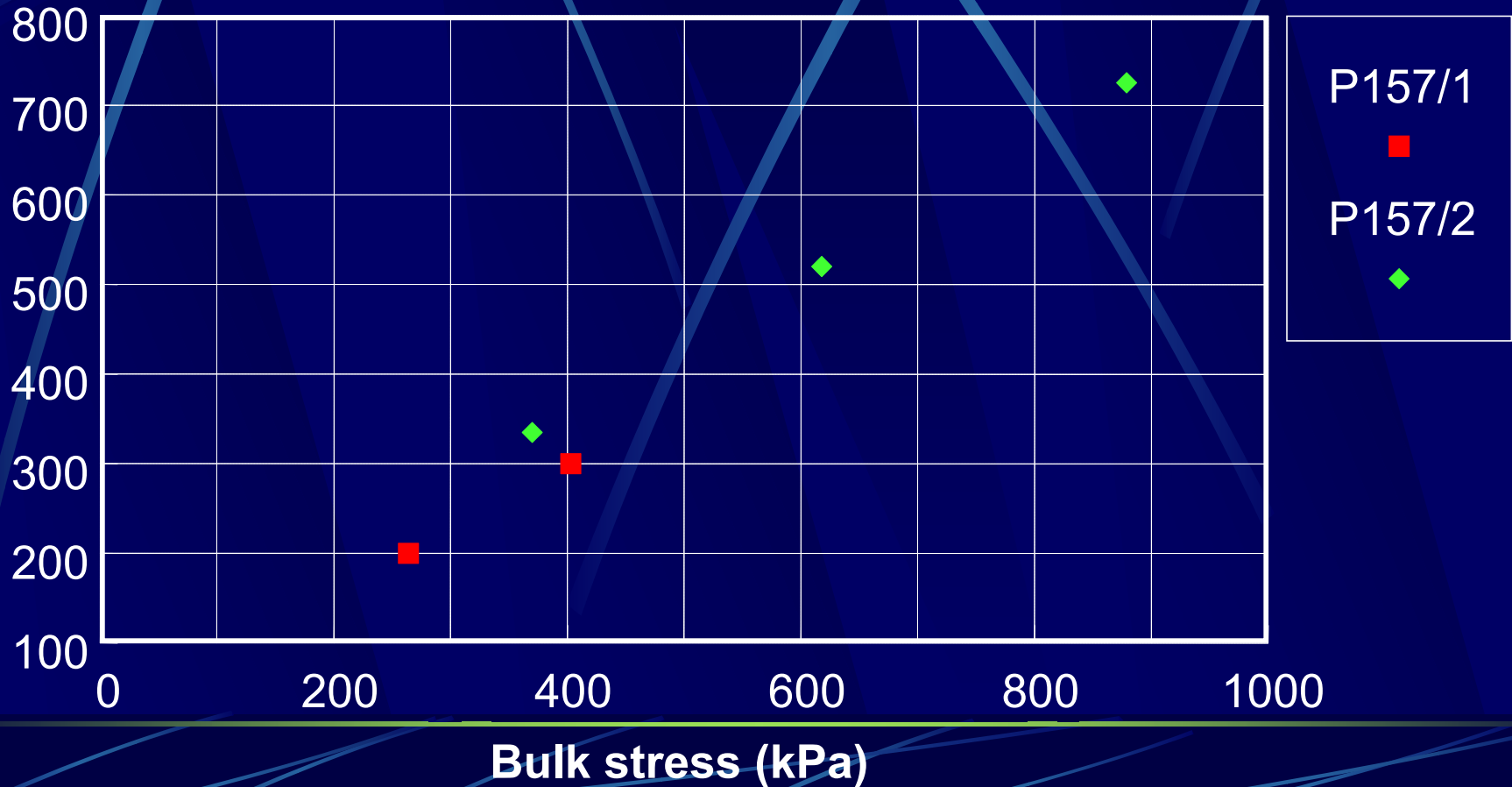
$$M_r = k \theta^n$$

$$M_r = k_0 \left( \frac{\theta}{P_a} \right)^{k_1} \left( \frac{\sigma_d}{P_a} \right)^{k_2}$$



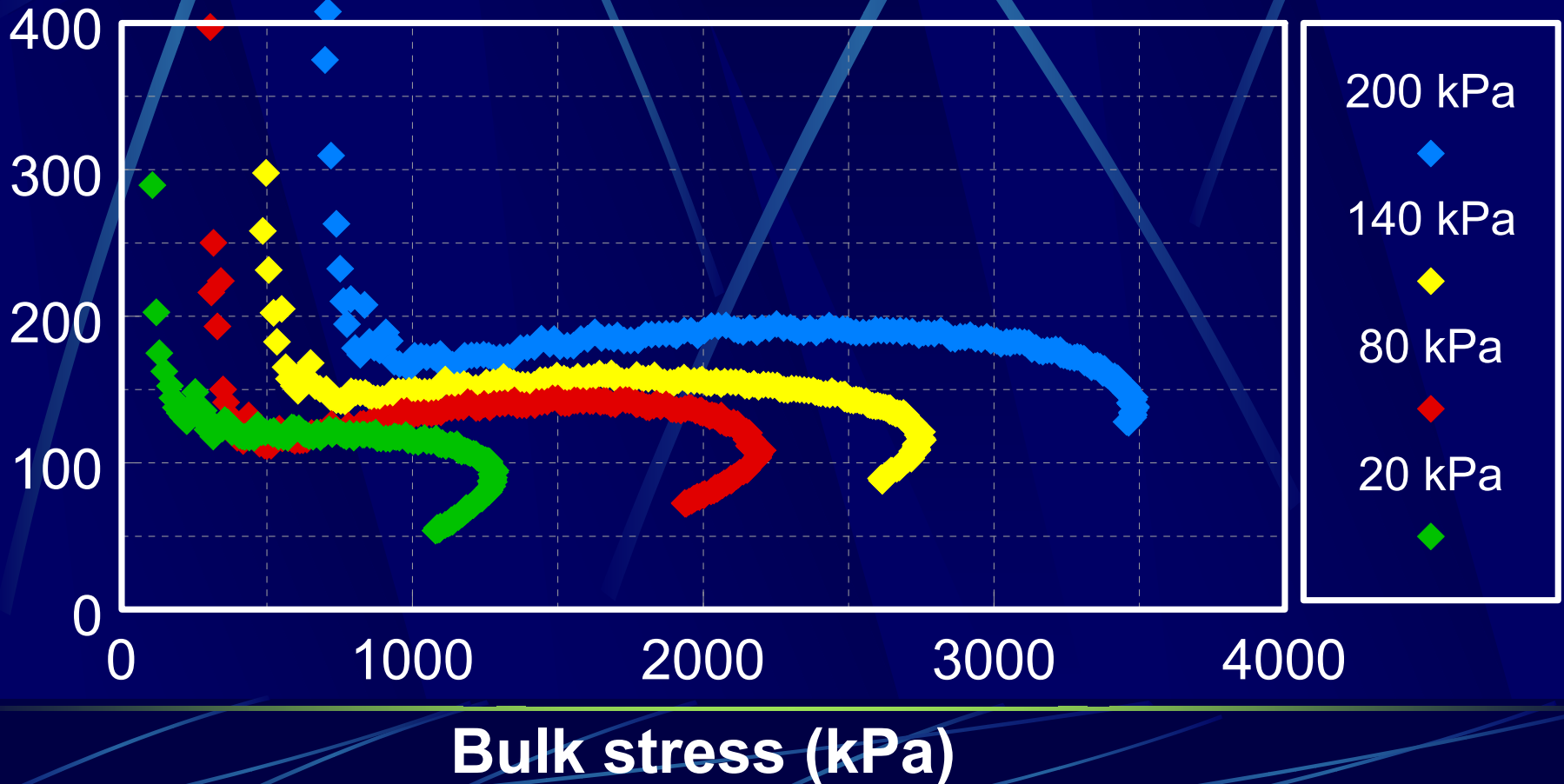
# Stress stiffening from MDD back-calculation

Resilient modulus (MPa)



# Appropriate confinement parameter

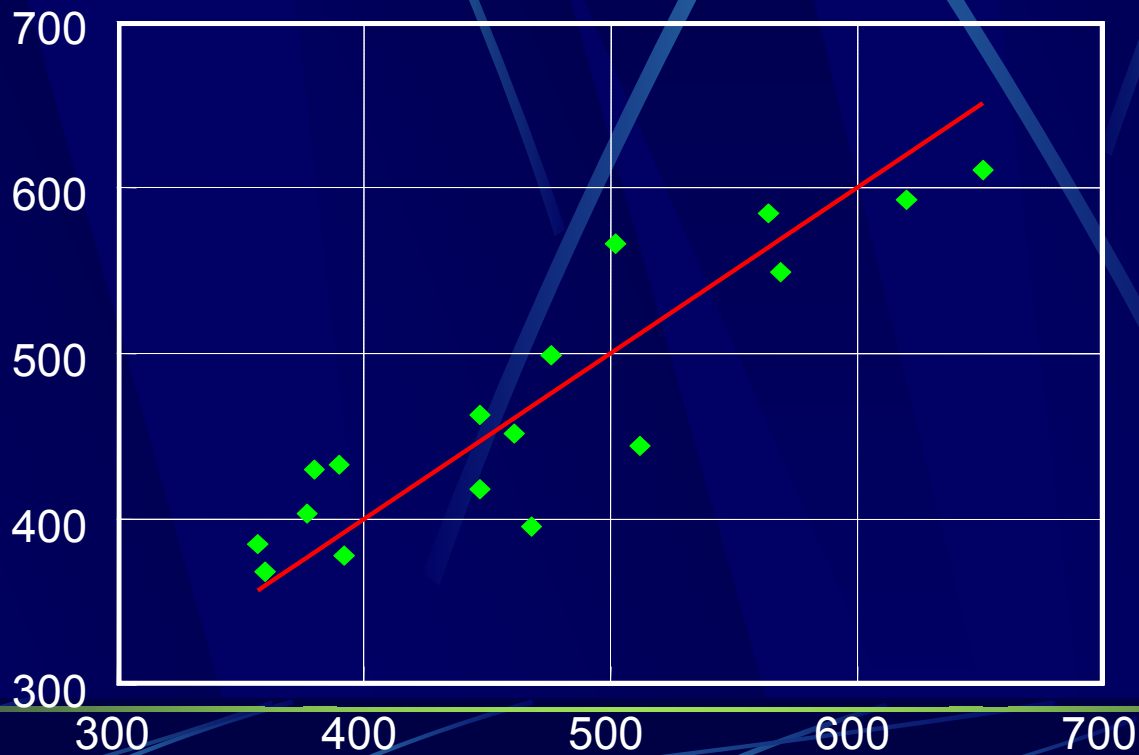
Secant stiffness (MPa)



# MDD depth deflection data: Deflection profile

- Dynamic triaxial results
- $M_R = -528 + 14.0 RD - 2.7 S + 0.83 \rho_3 - 0.87 SR$

Predicted  $M_r$  (MPa)



$R^2 = 81 \%$   
 $SEE = 45.4 \text{ MPa}$

# Conclusions: Resilient modulus

- Conclusions from laboratory results
  - Stress stiffening and softening behaviour
    - ◆ Important for modeling, no stress concentration
  - Relative density and degree of saturation largely determines resilient modulus
  - Typical dynamic resilient modulus values for crushed stone
    - ◆ 350 to 650 MPa depending on confinement, shear stress, relative density and degree of saturation
    - ◆ Compares well with HVS (300 - 700 MPa)



# Shear strength

Granular base/subbase layers:  
Combining laboratory and HVS data

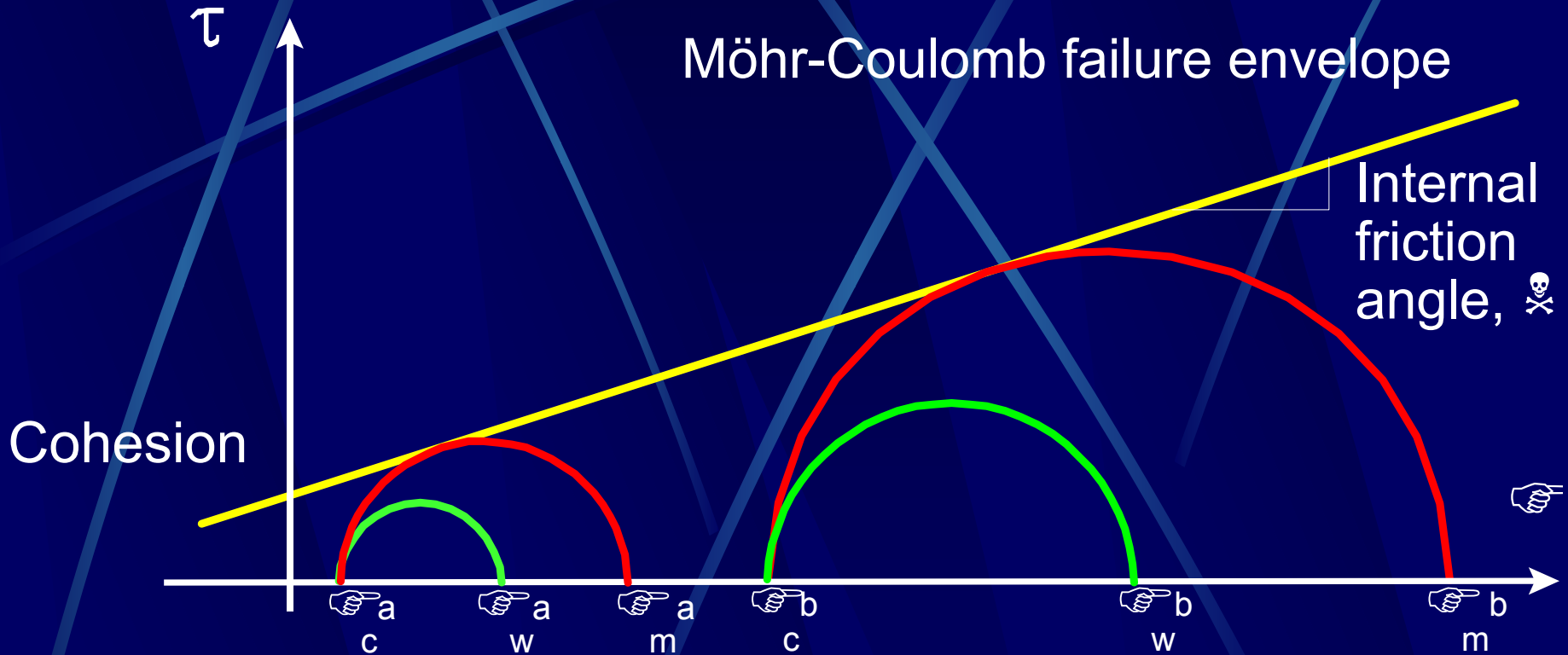
# Appropriate stress parameter

$$SR = \frac{\sigma_1^a - \sigma_3}{\sigma_1^m - \sigma_3} = \frac{\sigma_1^a - \sigma_3}{\sigma_3 \left( \tan^2 \left( 45^\circ + \frac{\phi}{2} \right) - 1 \right) + 2C \tan \left( 45^\circ + \frac{\phi}{2} \right)}$$

Shear strength parameters required

# Stress ratio

Möhr-Coulomb failure envelope

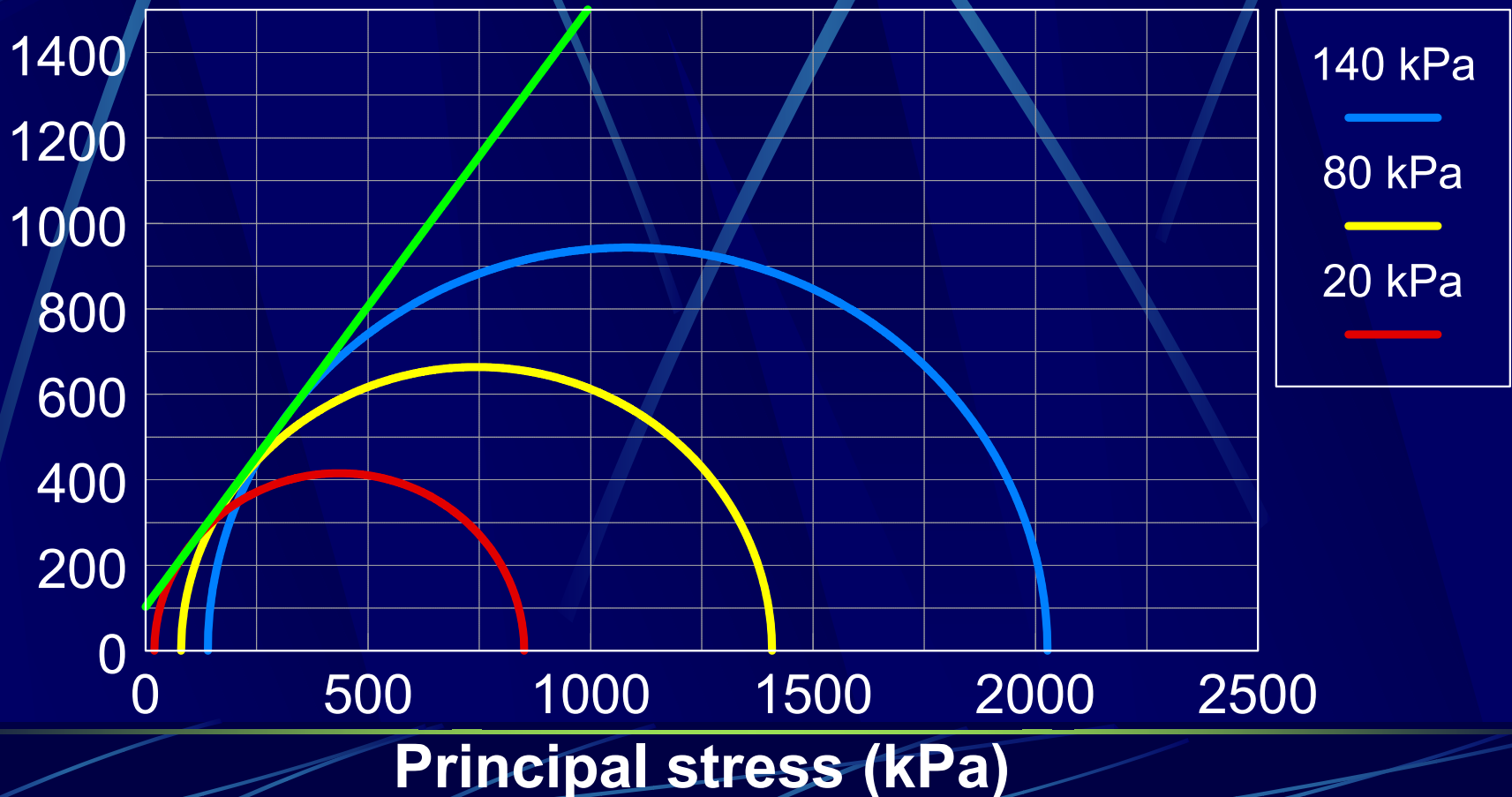


$$\text{Stress ratio } R = \frac{\overset{\text{a}}{\text{w}} - \overset{\text{a}}{\text{c}}}{\underset{\text{a}}{\text{m}} - \underset{\text{a}}{\text{c}}} = \frac{\overset{\text{b}}{\text{w}} - \overset{\text{b}}{\text{c}}}{\underset{\text{b}}{\text{m}} - \underset{\text{b}}{\text{c}}}$$

# Shear strength parameters

● Typical laboratory result

Shear stress (kPa)

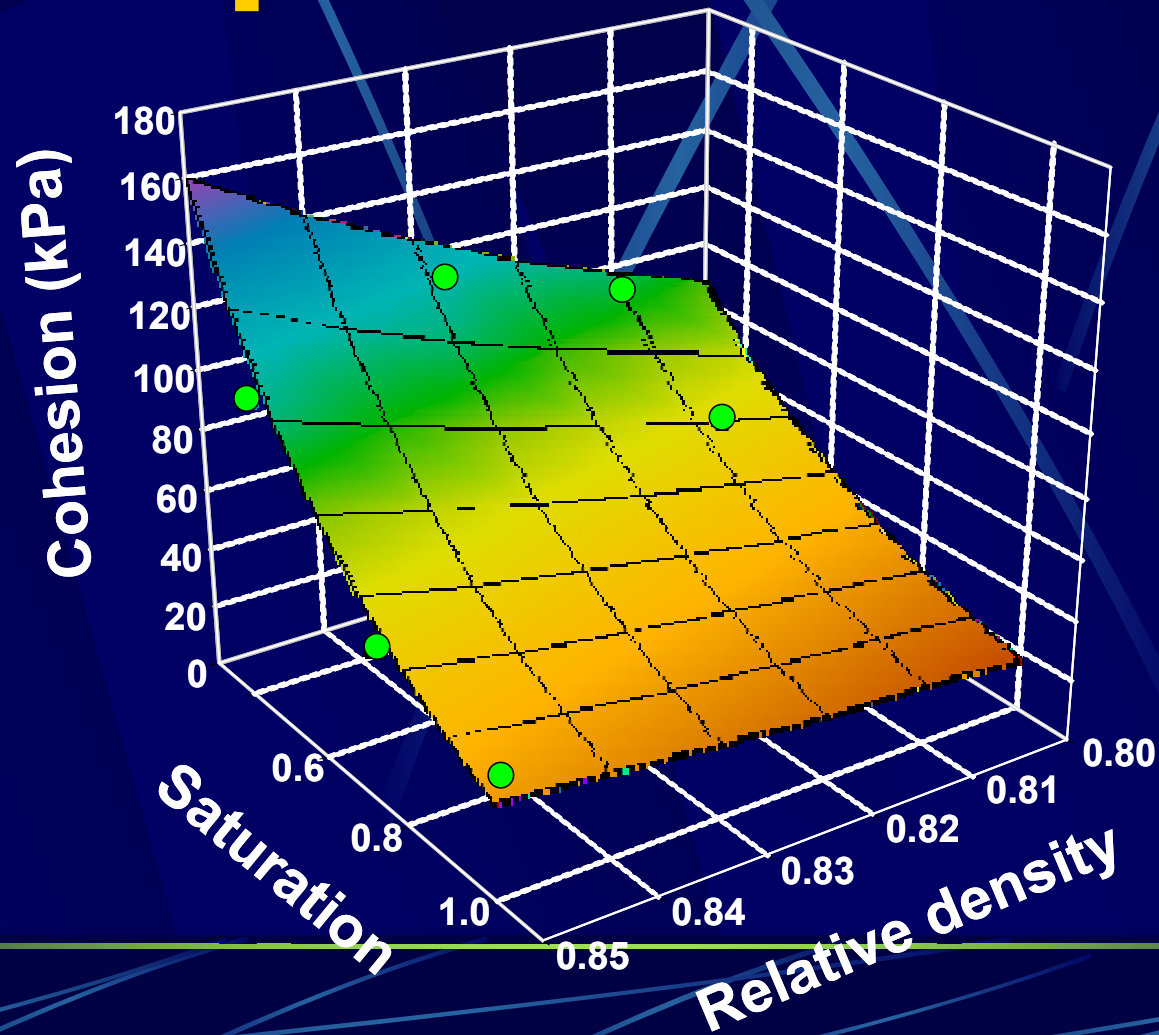




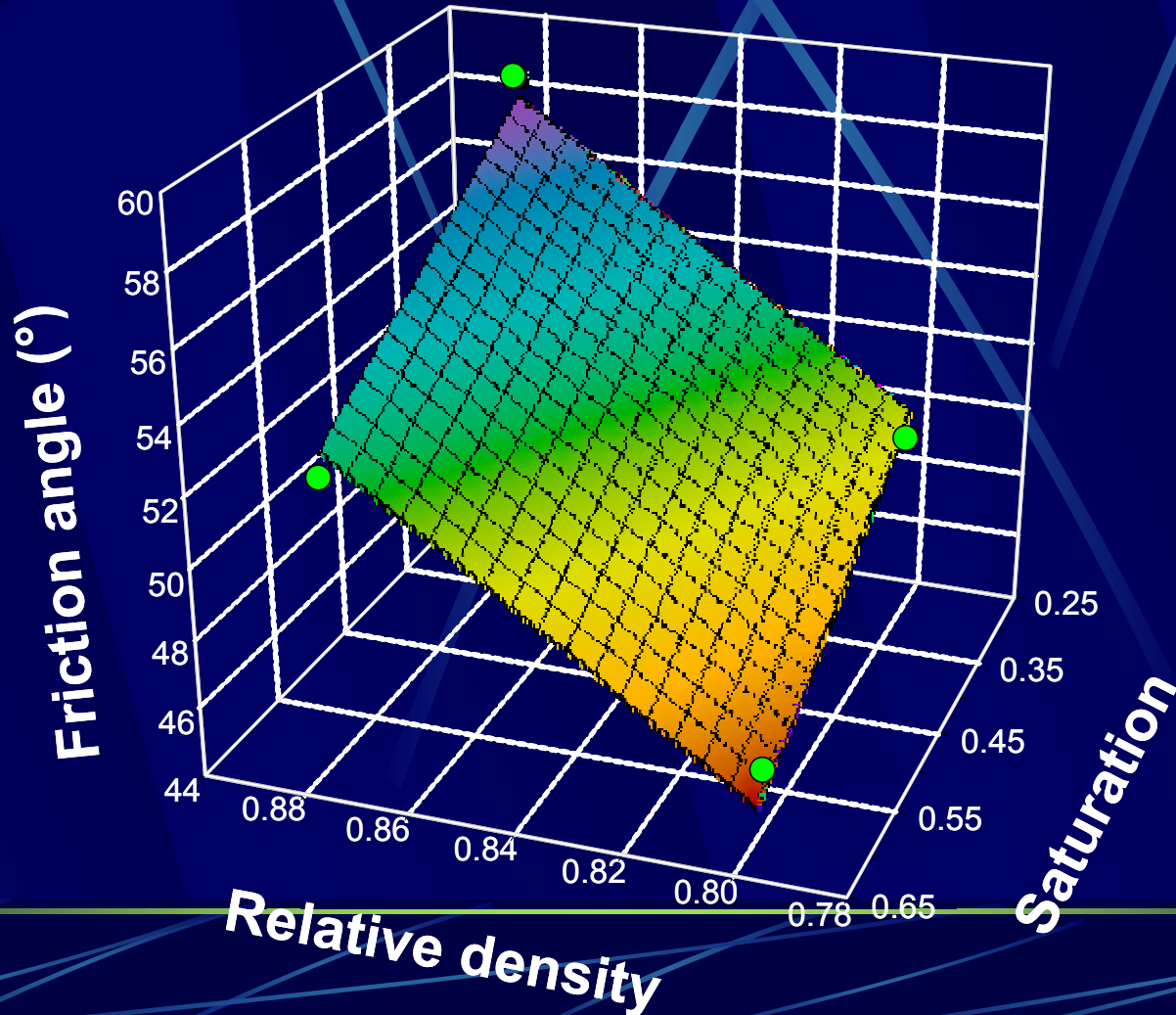
# Shear strength parameters

- Laboratory results - Maree 1982
  - Degree of saturation
    - ◆ Reduction in S
      - ◆ Significant increase in cohesion
      - ◆ No significant effect on friction angle
      - ◆ Significant increase in shear strength
  - Density
    - ◆ Increase in RD
      - ◆ No significant increase in cohesion
      - ◆ Significant increase in friction angle
      - ◆ Significant increase in shear strength
  - Grading and properties of coarse and fine fractions

# Shear strength parameters

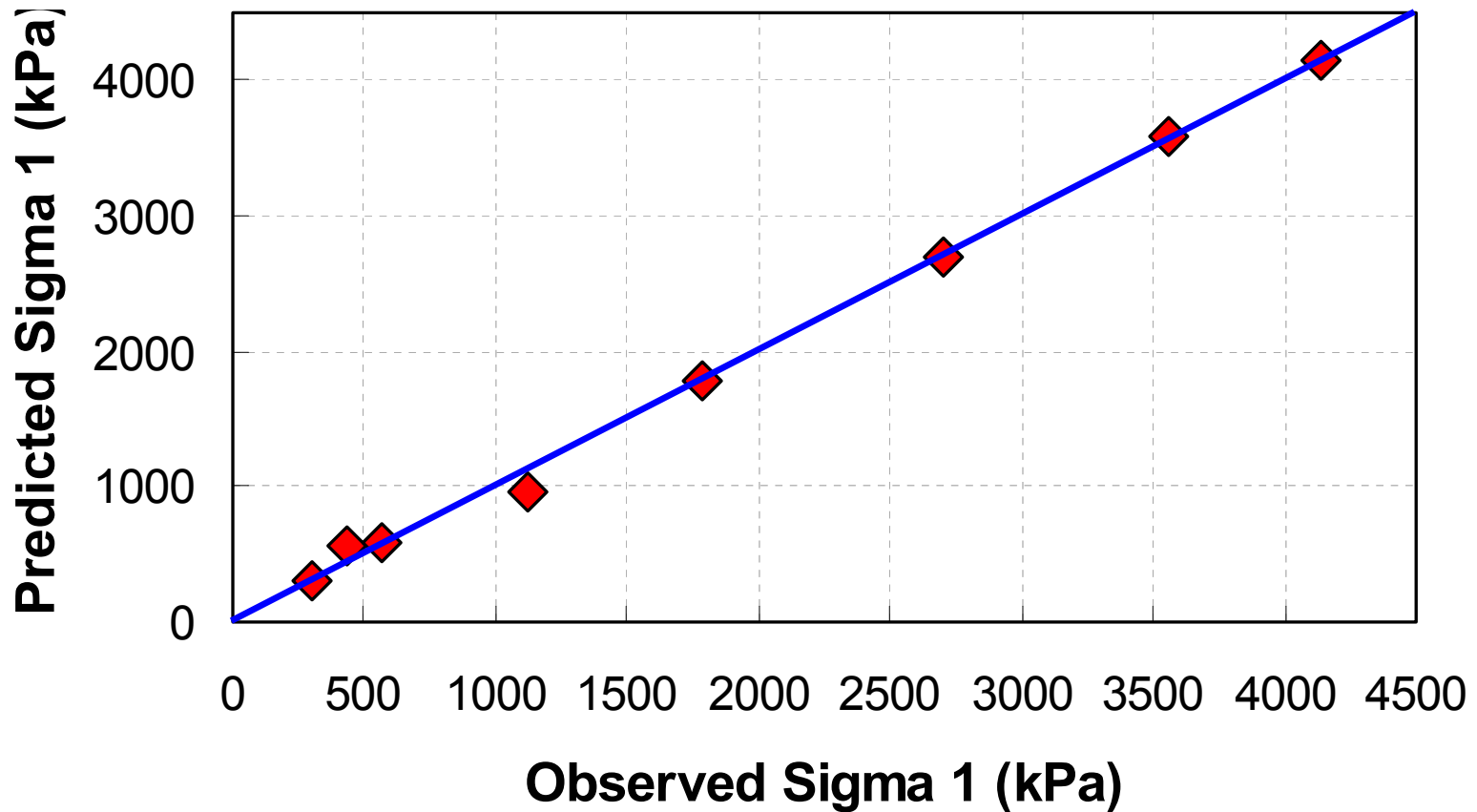


# Shear strength parameters



# Shear strength

Norite



# Shear strength parameters

## ● Conclusions from laboratory results

### ■ Correlation between

- ◆ Friction angle and cohesion

- ◆ Relative density (RD) degree of saturation (S)

### ■ Often interaction between shear strength parameters

- ◆ Simple regression models for shear strength

### ■ Need to investigate predictive models

- ◆ Particle size distribution

- ◆ Properties of course and fine fractions



# **Plastic deformation**

Granular base/subbase layers:  
Combining laboratory and HVS data

# Plastic deformation

## ● Stable

- Bedding-in

- Linear rate of deformation

## ● Unstable

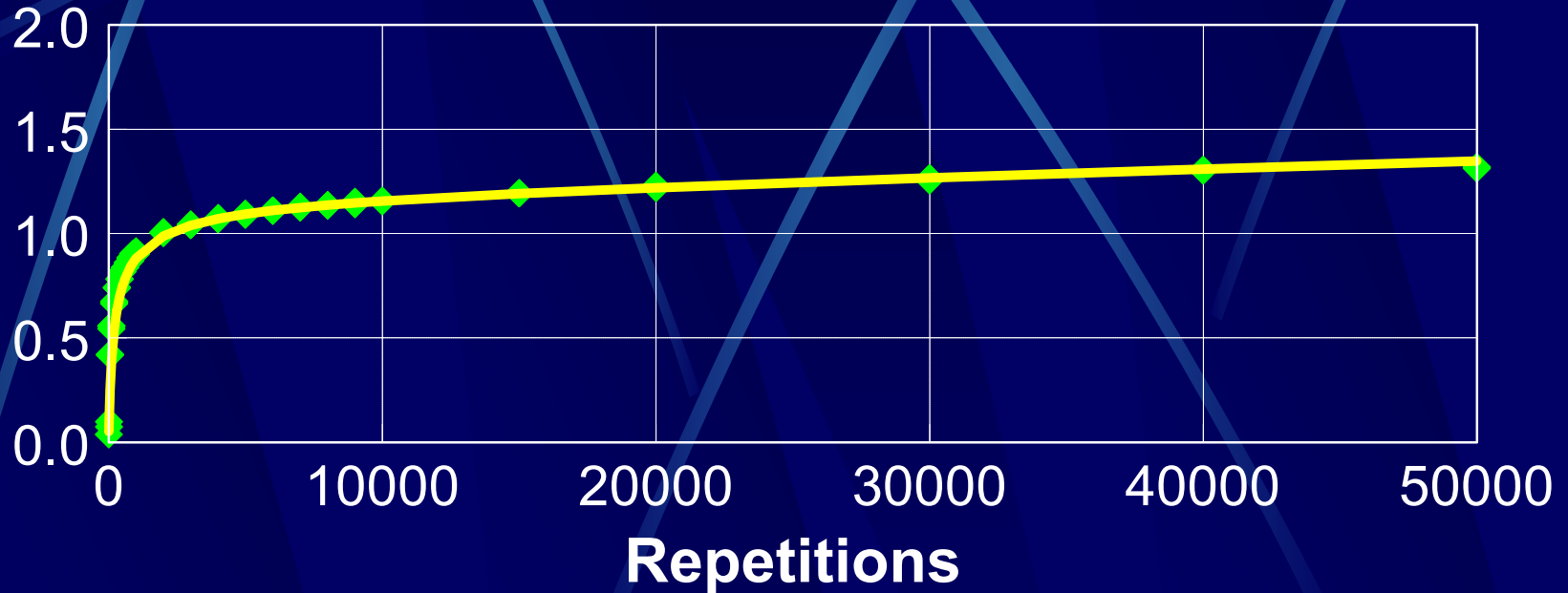
- Bedding-in

- Linear rate of deformation

- Exponential increase

# Stable permanent deformation

Permanent deformation (mm)



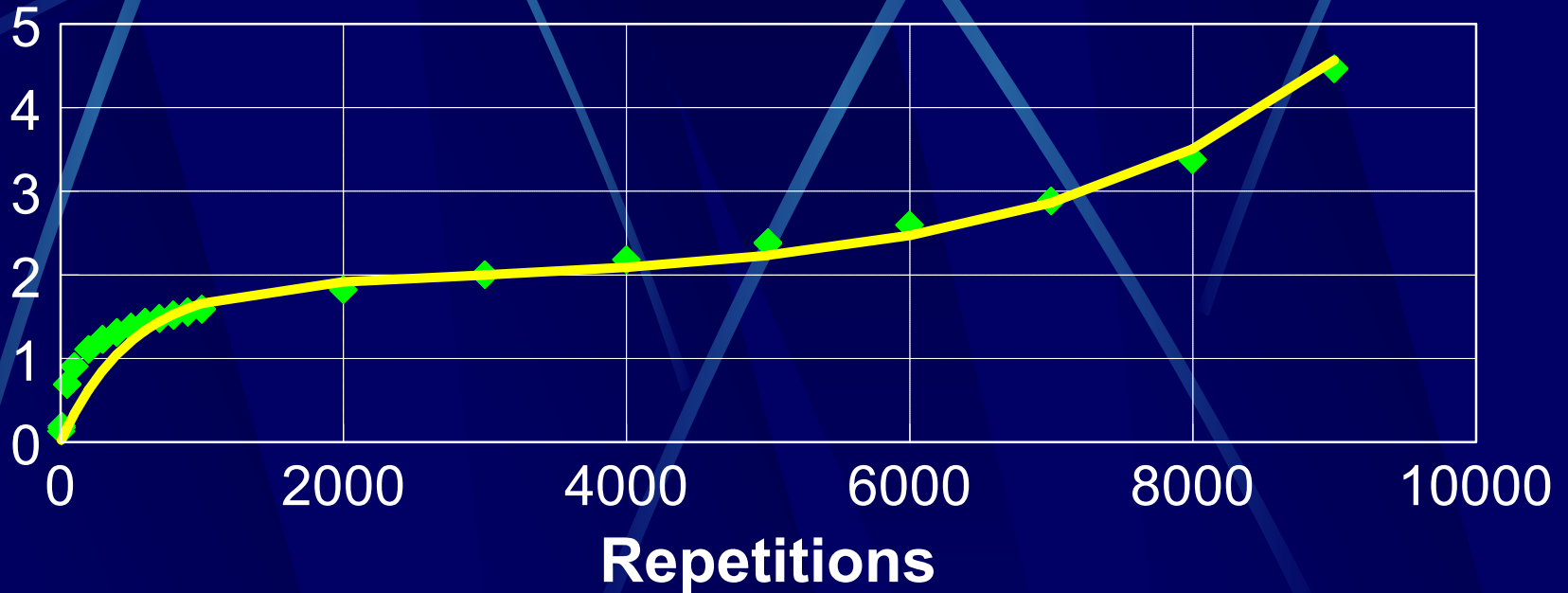
Sample Data Regression Model





# Unstable permanent deformation

Permanent deformation (mm)



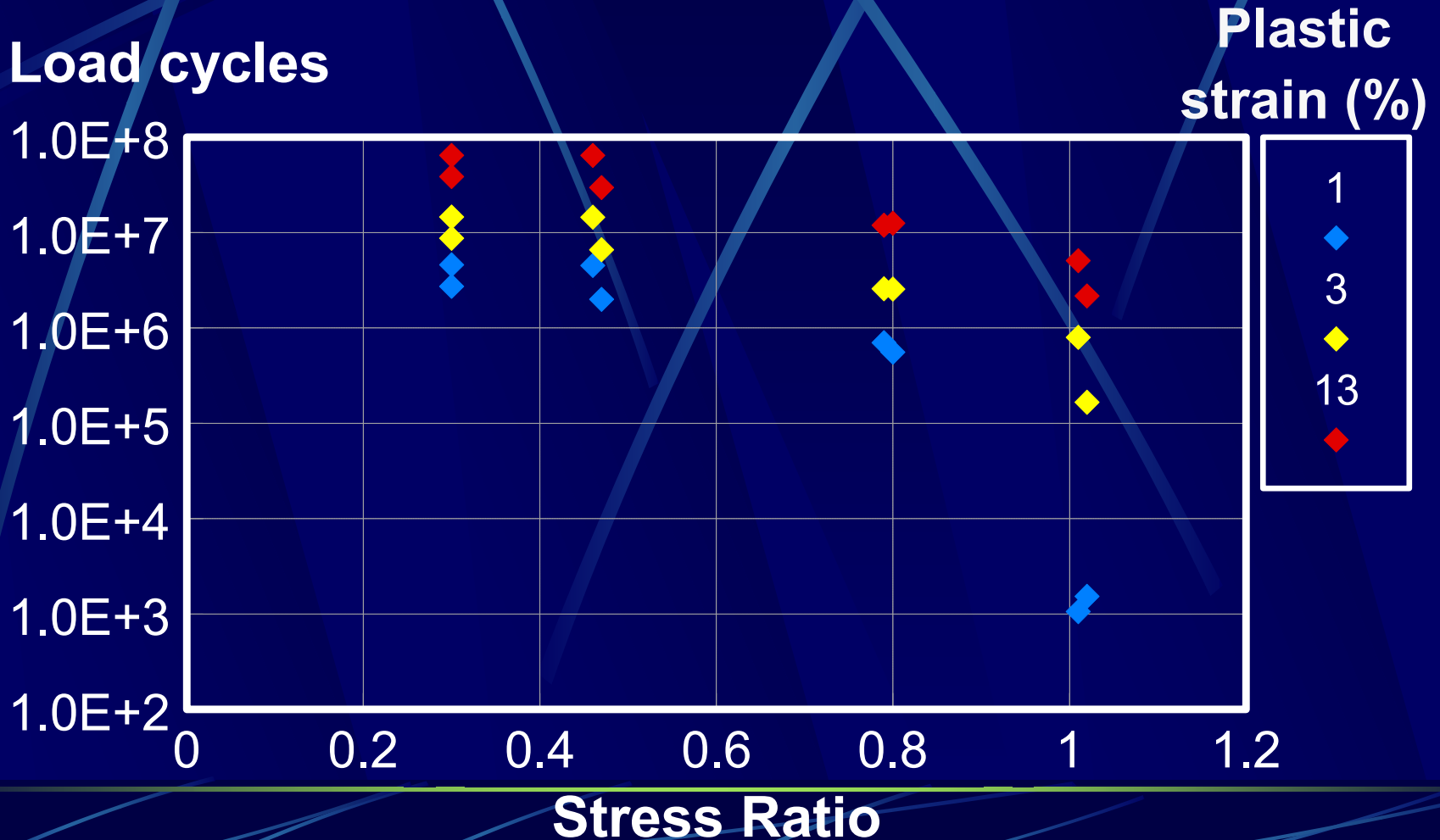
Sample data Regression model



# Permanent deformation Dynamic triaxial test

- Shear strength parameters known
- Dynamic triaxial tests
  - Two confining pressure levels
  - Three or more stress ratio values
- Non-linear regression analysis
  - $PD = f(\text{Number of repetitions, } N)$
- Determine N for selected levels of PD
- Plot N against stress parameter (S) to generate S-N plot

# Permanent deformation S-N plot



# Permanent deformation S-N plot

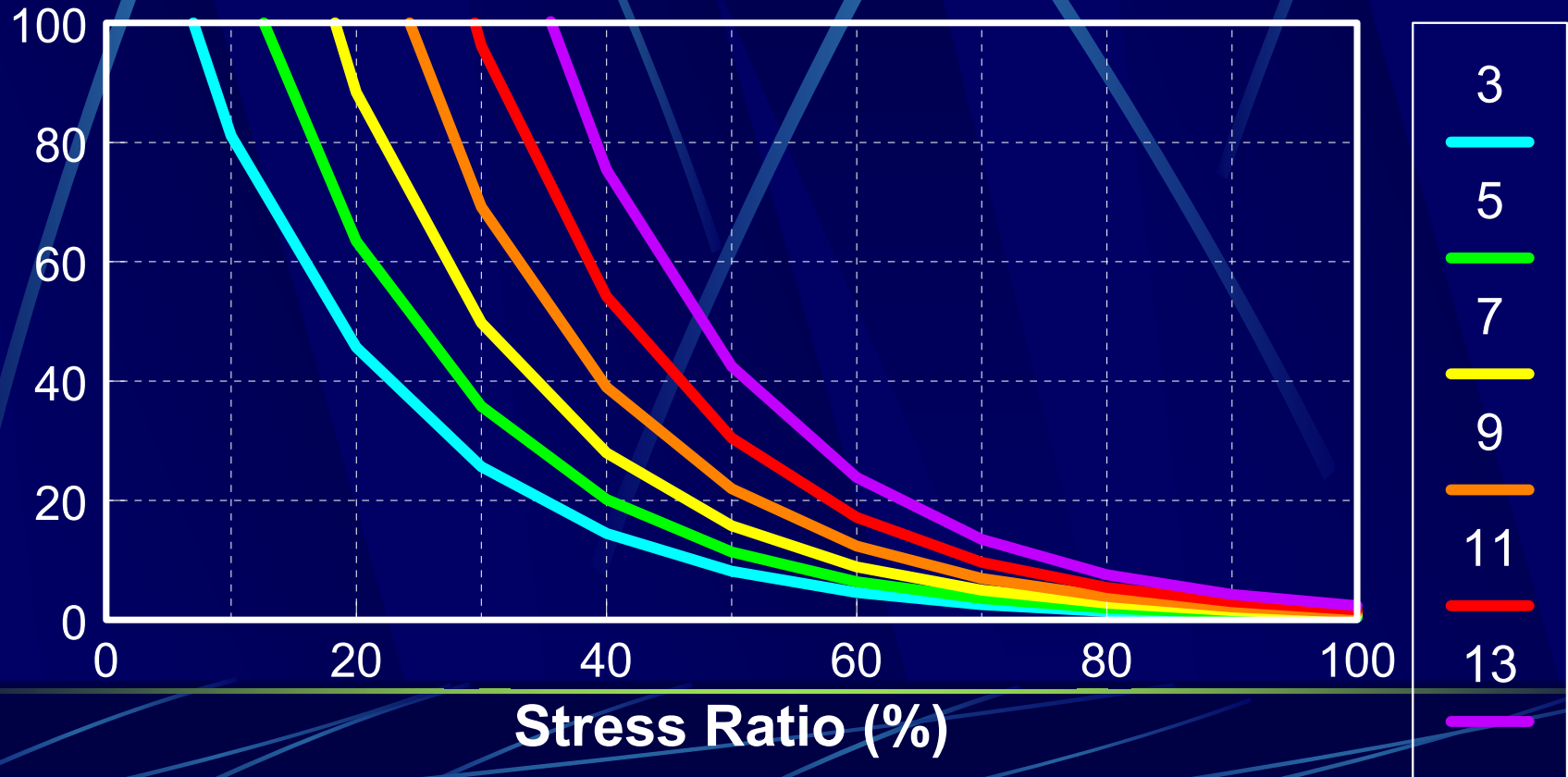
- Regression modeling of S-N data provides contour plots on 3-dimensional plastic strain model
- Contour plots used as design transfer functions
  - Effects of density and saturation included

# S-N design model

## 84 % AD, 45 % S

Bearing Capacity (Repetitions)  
Millions

Plastic  
strain (%)

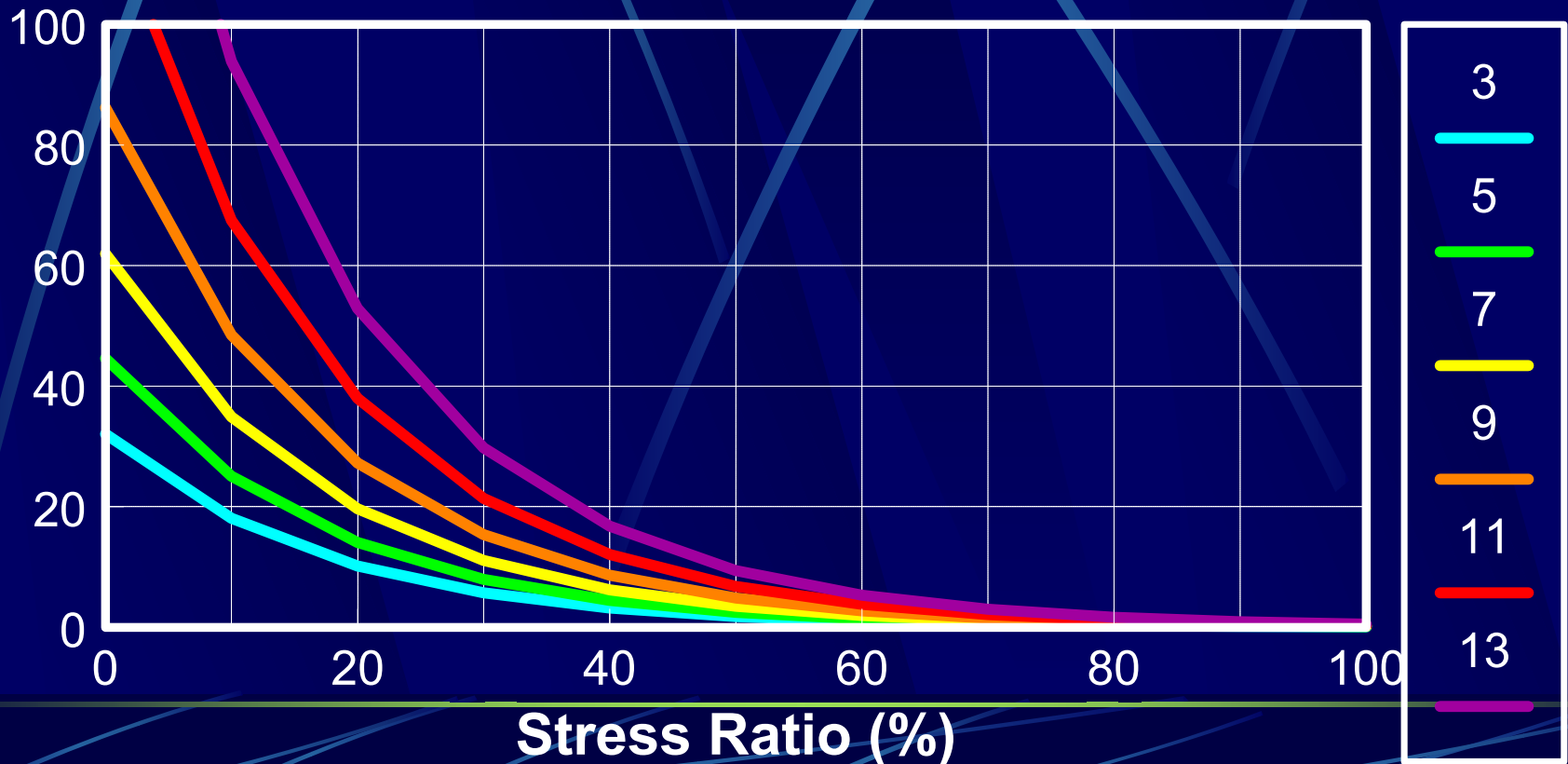


# S-N design model

## 84 % AD, 55 % S

Bearing Capacity (Repetitions)  
Millions

Plastic  
strain (%)



# Conclusions

## Permanent deformation

- Permanent deformation or plastic strain of granular materials
  - Degree of saturation
  - Relative density
  - Combined shear and confinement stress

# **A comparison between laboratory and HVS permanent deformation models**



Granular base/subbase layers:  
Combining laboratory and HVS data



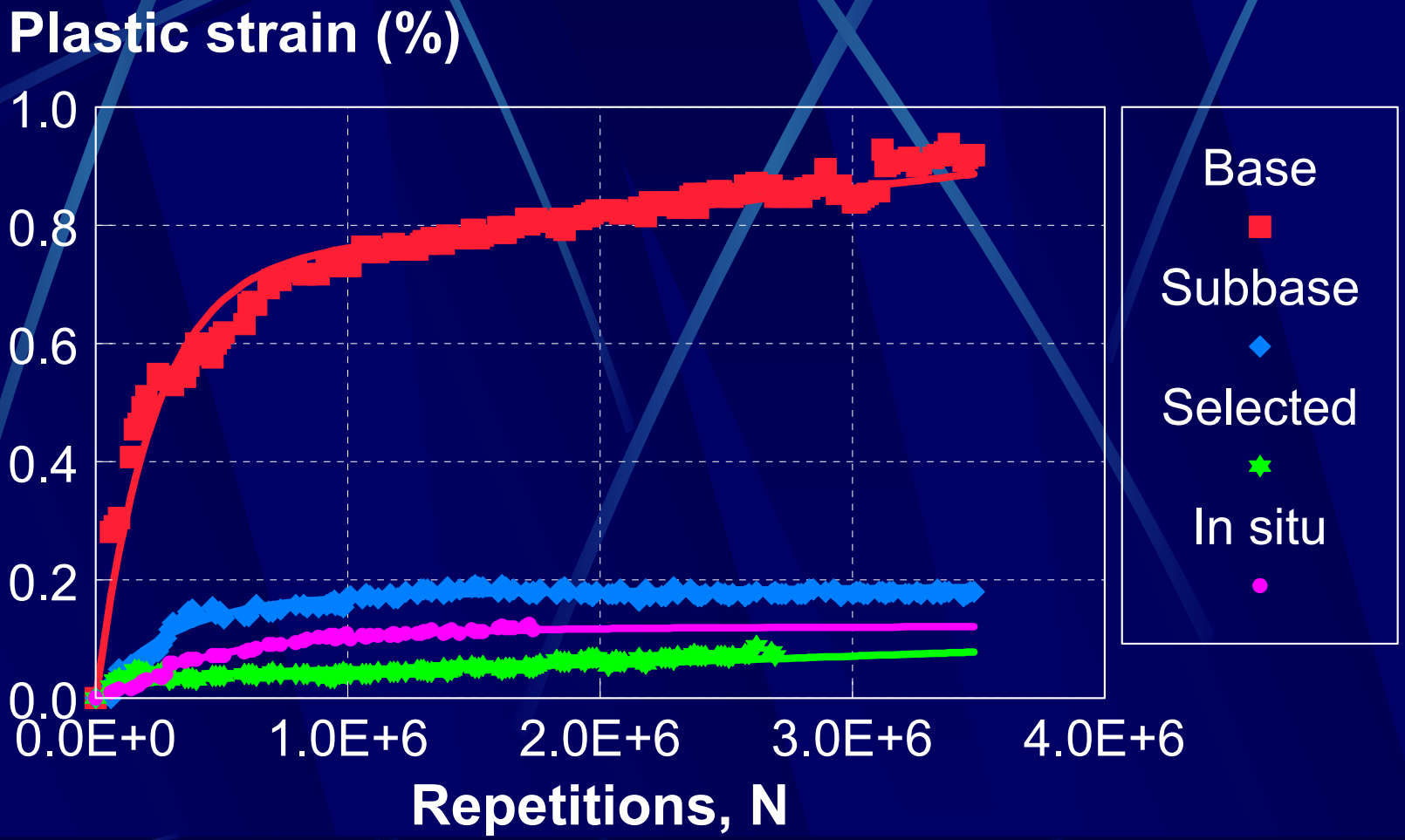
# Process

- Determine plastic deformation of base layers from MDD permanent displacement data
  - Subtract permanent displacement of module at bottom of layer from that of the module at the top of the layer
  - Fit non-linear model
  - Solve for “N” that would result in 10 mm base layer permanent deformation
- Back-calculation of MDD deflection data
  - Resilient modulus
  - Calculate stress ratio at mid-depth of layer using shear strength calibrated for density and saturation
- All this data available for two load levels

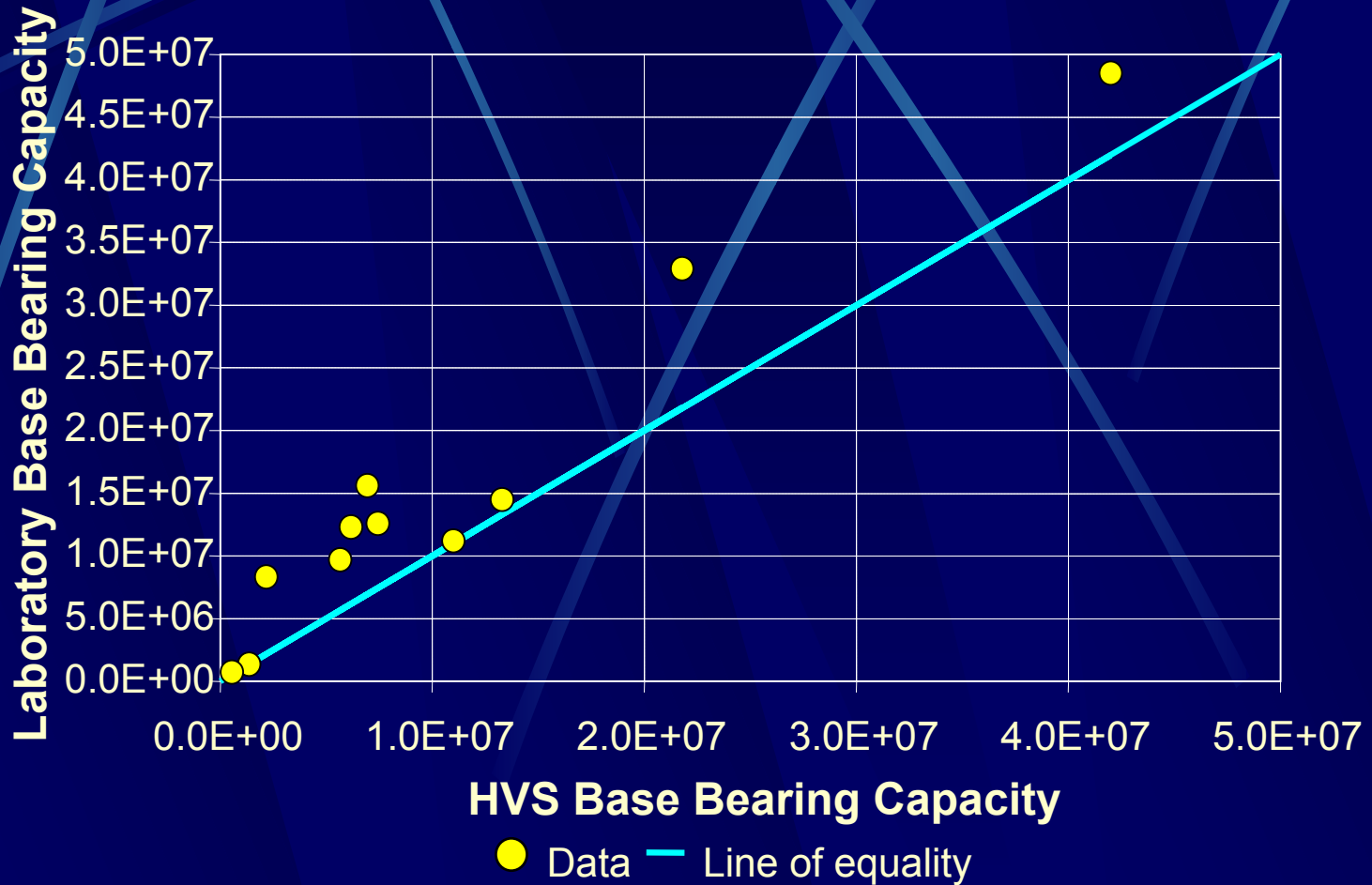
# Process (continued)

- Using the known layer thickness, calculate the plastic strain that is equivalent to 10 mm permanent deformation
- Enter stress ratio and plastic strain in the laboratory model
  - Solve for “N”
- Compare “N” from field testing with “N” from laboratory model

# Permanent deformation result from field testing



# Base bearing capacity: HVS and laboratory



# In summary: Granular layers

- Biggest problem
  - Calculation of correct stress ratio in pavement base/subbase layers
  - Non-linear, stress-dependent model calibrated for density and saturation
- Separate elastic and plastic response
- Move away from linear Mohr-Coulomb shear strength parameters
  - Shear strength calibrated for density and saturation
- Established concepts need to develop and refine
  - “Surrogate” resilient modulus and shear strength models